

Best Before? Expiring Central Bank Digital Currency and Loss Recovery¹

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¹Views expressed do not necessarily reflect official positions of the Bank of Canada.

As central banks explore issuing digital cash substitutes...

- Kosse and Mattei (2022); Group of Seven Central Banks (2020); Bank of Canada (2020); European Central Bank (2021)

...the focus is increasingly shifting from **whether to issue**...

- Barrdear and Kumhof (forthcoming); Brunnermeier and Niepelt (2019); Andolfatto (2020); Chiu et al. (2019); Fernández-Villaverde et al. (2021); Keister and Sanches (forthcoming); Williamson (forthcoming)

...towards **design aspects** of CBDC

- **Security** (Kahn et al., 2020)
- **Interest** (Barrdear and Kumhof, forthcoming; Jiang and Zhu, 2021)
- **Privacy** (Garratt and Van Oordt, 2021; Lee and Garratt, 2021)
- **Programmability** (Kahn and Van Oordt, 2021)
- **Multiple features** (Li, 2021; Huynh et al., 2020; Bijlsma et al., 2021)
- **Expiry date and personal loss recovery**: This paper
 - Note: not to stimulate spending (Andolfatto, 2020)

An important advantage of physical cash: Payments can be made without power or network connectivity.

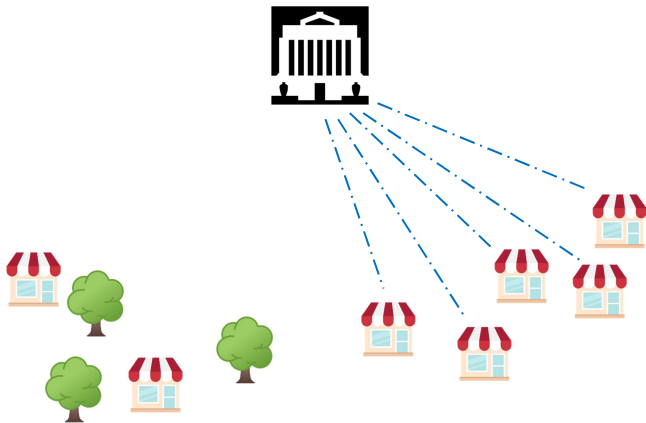
- Developing countries
- Remote locations
- Cyberattacks or technological failures
- Natural disasters
- Geopolitical conflicts

Central banks aim for similar offline capability in electronic cash substitute. Argues for device-based storage.

Ruling out double-spending requires

- ① storing balances uniquely in (tamper-resistant) device, and
- ② separation of funds that can be spend with that device

Facilitating offline payments and double-spending



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- 2 separation of funds that can be spend with that device

Consequence: Loss of device implies loss of funds...
(analogy to cash)

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This paper: Can we reduce the cost of digital cash losses?

Facilitating offline payments and double-spending



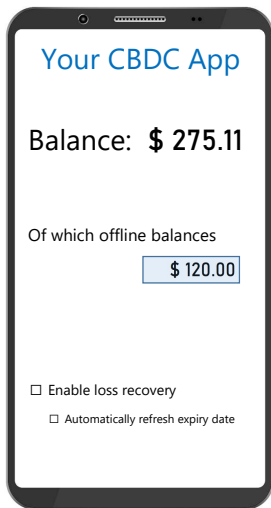
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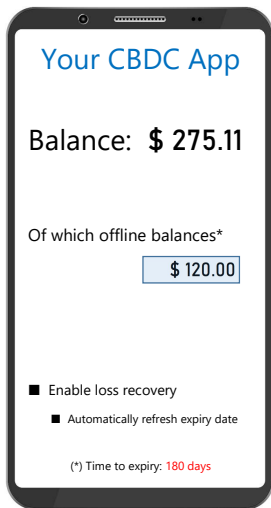
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This paper: Can we reduce the cost of digital cash losses?

- Yes, we can do so with an expiry date.
- Automatically reimburse consumers expired offline balances
- Interesting economic trade-offs.





Expiry date and loss recovery

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But who “lost” the cash?

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We consider two information structures:

- **“Higher privacy”**
 - Syncing payor’s device does not reveal whether and where payor spent offline balances
 - Onus is on payees to deposit balances before expiry date

Expiry date and loss recovery

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But who “lost” the cash?

We consider two information structures:

- **“Higher privacy”**

- Syncing payor’s device does not reveal whether and where payor spent offline balances
- Onus is on payees to deposit balances before expiry date

- **“Lower privacy”**

- Syncing device reveals whether and where payor spent offline balances.
- Payee still wants to deposit balances before expiry date
- If payor’s device reveals offline balances were used to pay a payee without being deposited, then that payee is reimbursed

- Loss recovery with expiry date could have a substantial positive impact on demand for offline balances and welfare.
- Less costly to set a longer than optimal expiry date than to set an expiry date that is too short.
- More information-sharing between consumers and the central bank can improve loss recovery but has an ambiguous impact on social welfare.

- Small model (understand trade-offs)
- Infinite horizon model (idea of quantitative impact)
- Conclusion

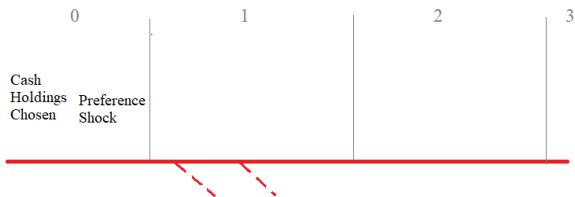
Goal: Illustrate trade-offs related to the expiry date

Cash: a money balance that can be used for offline payments

- Stored-value in a payment card or smartphone chip

Cash “insures” consumption during outages, but is subject to losses.

Timeline: $t = 0$



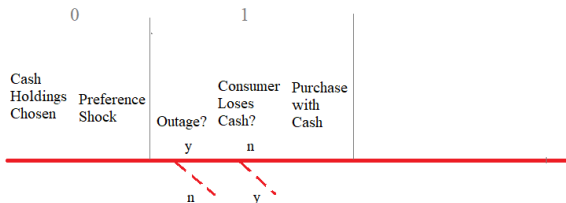
At $t = 0$, the consumer decides how much cash to hold

- Online balances pay interest i , cash does not

A preference shock is realized

- Consumer either want to consume one or two units at $t = 1$

Timeline: $t = 1$



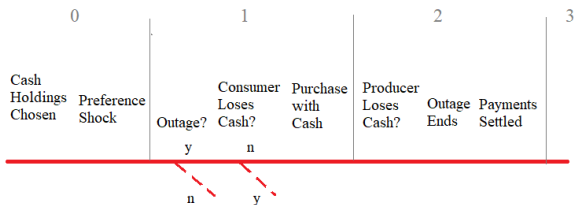
Two independent random shocks realized

- An outage disrupting the connectivity for payments may occur
- Consumer may lose cash (probability δ)

Consumers buy goods from producers

- If no outage, both online balances and cash can be spent
- If outage, only cash can be spent and consumption will be bounded by cash holdings

Timeline: $t = 2, 3$



At $t = 2$:

- Producer may lose offline cash with probability η
- Outage ends if there is one
- Withdraw/deposit cash and online payments arrive

At $t = 3$, everybody enjoys counting their money

If paid with offline payments, competitive producers charge a premium, to compensate for potential losses; thus consumer's default payment instrument is online.

Consumers hold offline money as a precaution, to facilitate trade during outages. Holdings limited by

- Chance of loss
- Inconvenience or opportunity cost of sequestering on the device (modeled as interest rate differential)

How to account for lost cash?

- Lost cash is a windfall profit for the central bank
- Reimbursing lost cash is costly to the central bank
- Net welfare effect of reimbursed cash is zero in the aggregate

In equilibrium, social welfare equals expected number of units consumed per consumer

Consumers' cash holdings

Hold cash to purchase 1 or 2 units if the benefit exceeds the cost.

- Benefit comes from ability to consume during an outage
- Cost includes foregone interest and cost of cash losses: $i + \delta$

Constraint for carrying enough cash to purchase a second unit is more demanding

- Only with probability one-half consumers are interested in consuming the second unit

Social welfare:

- Reducing likelihood of losing cash would increase welfare, because increases buyer willingness to hold cash, and thus increases offline trade.

Results: Cash expires too quickly (shelf life: 1 period)

Acceptance:

Cash expires in period 2 before the producer can deposit cash

- Central bank would automatically reimburse the consumer

Producers reject cash

Cash holdings:

- None

Social welfare:

- No transactions occur during outages...
- Reduced to the level in a no-cash environment

Results: Cash expires slowly (shelf life: 2 periods)

Acceptance:

Producers know outage will end before expiry date, so willing to accept cash.

Cash holdings:

Consumers may hold more cash because the cost of cash losses is reduced

- Consumers are reimbursed for lost cash with some delay
- Cost of carrying cash is

$$i + \delta(1 - \beta^2)$$

Social welfare:

- Strictly improves whenever equilibrium cash holdings are higher
- With high privacy this is generally the case

After an outage, would consumers be willing to reconnect?

- Consumers who spent all offline cash do not reconnect
- Consumers who have unspent cash reconnect iff $i \geq \eta$
(interest foregone vs windfall if producer loses cash)

Two situations:

- If $i < \eta$, increase in cost of precautionary cash holdings...
Reduction in social welfare
- If $i \geq \eta$, some producers charge lower “cash” prices because of reimbursement for cash losses: *May improve social welfare*

Small model helps to better understand economic trade-offs

How about the quantitative impact?

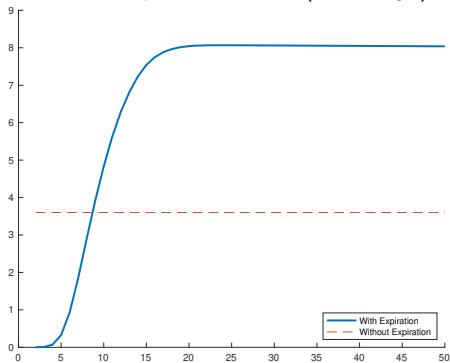
Calibration of more complex model to get a rough idea...

| Parameter | Daily value | (annualized) |
|--|--------------------|---------------------|
| Discount factor (β) | 0.99990 | 0.96 |
| Risk aversion (σ in $u(c) = \frac{c^{1-\sigma}}{1-\sigma}$) | 0.70 | |
| Loss probability consumer (δ) | 0.0004858 | 0.162 |
| Loss probability producer (η) | 0.0004858 | 0.162 |
| Outage probability (λ) | 0.00061 | 0.20 |
| – Length: Poisson distribution | 9.555 | 0.0262 |

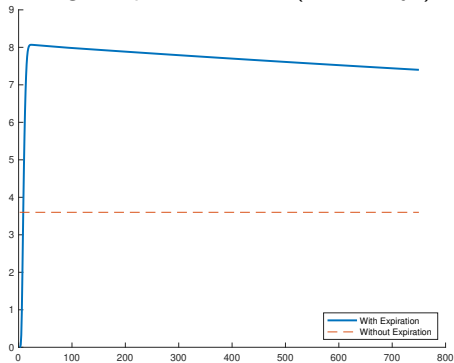
Conduct online survey: 16.2% (8.4%) people lost or damaged their cards (phones) in the previous year

Cash holdings as a function of the time to expiration

Shorter expiration dates (0-50 days)



Longer expiration dates (0-750 days)

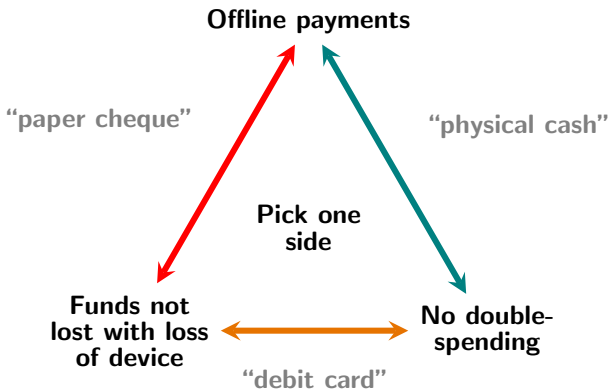


- Loss recovery based on introducing an expiry date could have a substantial positive impact on consumer demand for offline digital currency balances.
- The cost of setting a longer than optimal expiry date is small; setting an expiry date that is too short has a large negative impact.
- More information sharing between consumers and the central bank can improve loss recovery but has an ambiguous impact on social welfare.

Thank you

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Offline payment trilemma

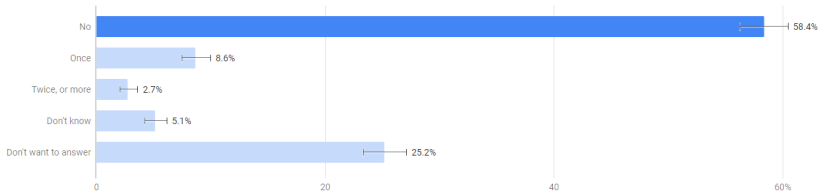


Some survey evidence in the US

(probability of losing balance during a year: on card $\pm 16\%$, on phone $\pm 8\%$)

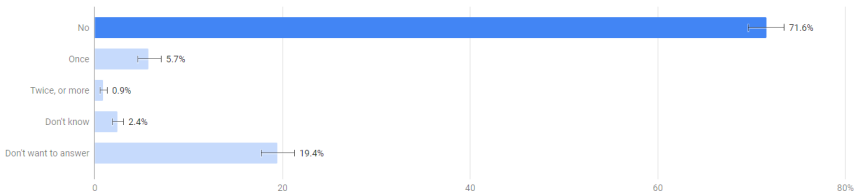
Over the past 12 months, did you replace or cancel a payment card (for example, a debit or credit card) because it was damaged, physically stolen or lost?

1,146 respondents

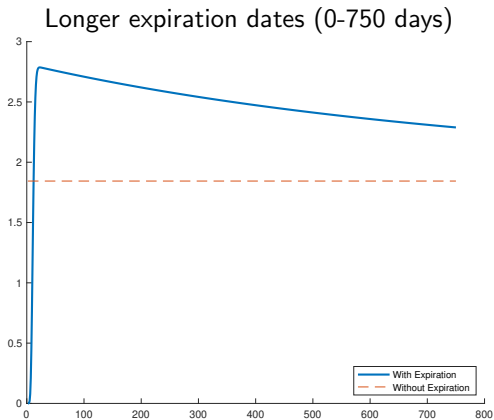


Over the past 12 months, was your smart phone stolen, permanently lost, or broken so that you could no longer start it?

1,118 respondents



Cash holdings with low discount factor ($\beta = 0.76$)



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